

**B.R. Ambedkar Bihar University, Muzaffarpur**  
**Directorate of Distance Education**  
**P.G. 2nd Semester Examination 2016 (Semester 2015-17)**  
**Subject:- Mathematics**  
**Assignment / Internal Assessment (दत्त कार्य)**  
**(Answer all the questions) Full Marks = 30**  
**Paper-V**

1. Define range of a projection. Prove that two projections E and F have the same range if and only if  $EF = F$  and  $FE = E$ .
  2. State and prove Sylvester's Theorem.
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**Paper-VI**

1. Define Analytic and Regular functions. State and prove that necessary and sufficient conditions for  $f(z)$  to be analytic.
  2. State and prove Morera's theorem.
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**Paper-VII**

1. Solve the following reducing equations into one equation of higher order.  
(i)  $\frac{dx}{dt} = y, \frac{dy}{dt} = x$   
(ii)  $\frac{dx}{dt} = 3x-2y, \frac{dy}{dt} = 2x-y$ .
  2. State and prove Peano's Existence theorem and its corollary.
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**Paper-VIII**

1. If X is any set, then prove that  $\text{Card } P(X) = 2^{\text{Card } X}$ ,  $P(X)$  being the powerset of X.
2. State and prove well-ordering theorem.